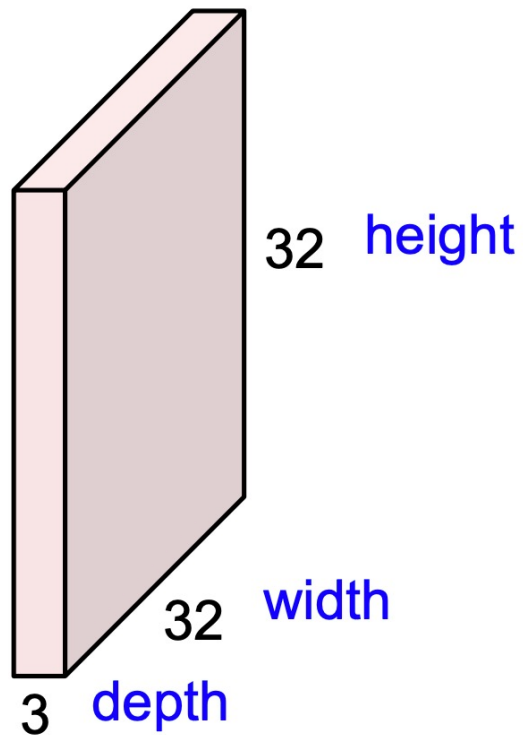




# Convolutional Neural Network (CS.231)

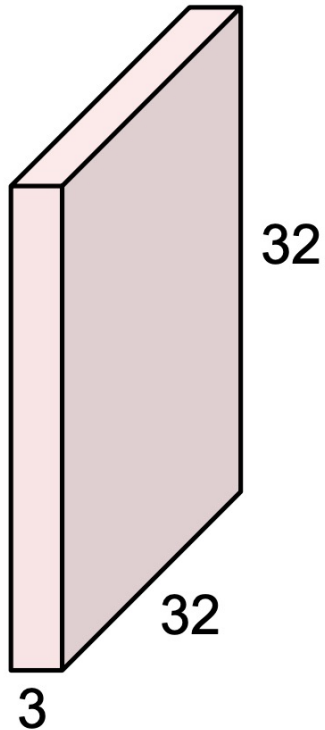
# Convolution Layer

32x32x3 image -> preserve spatial structure



# Convolution Layer

32x32x3 image



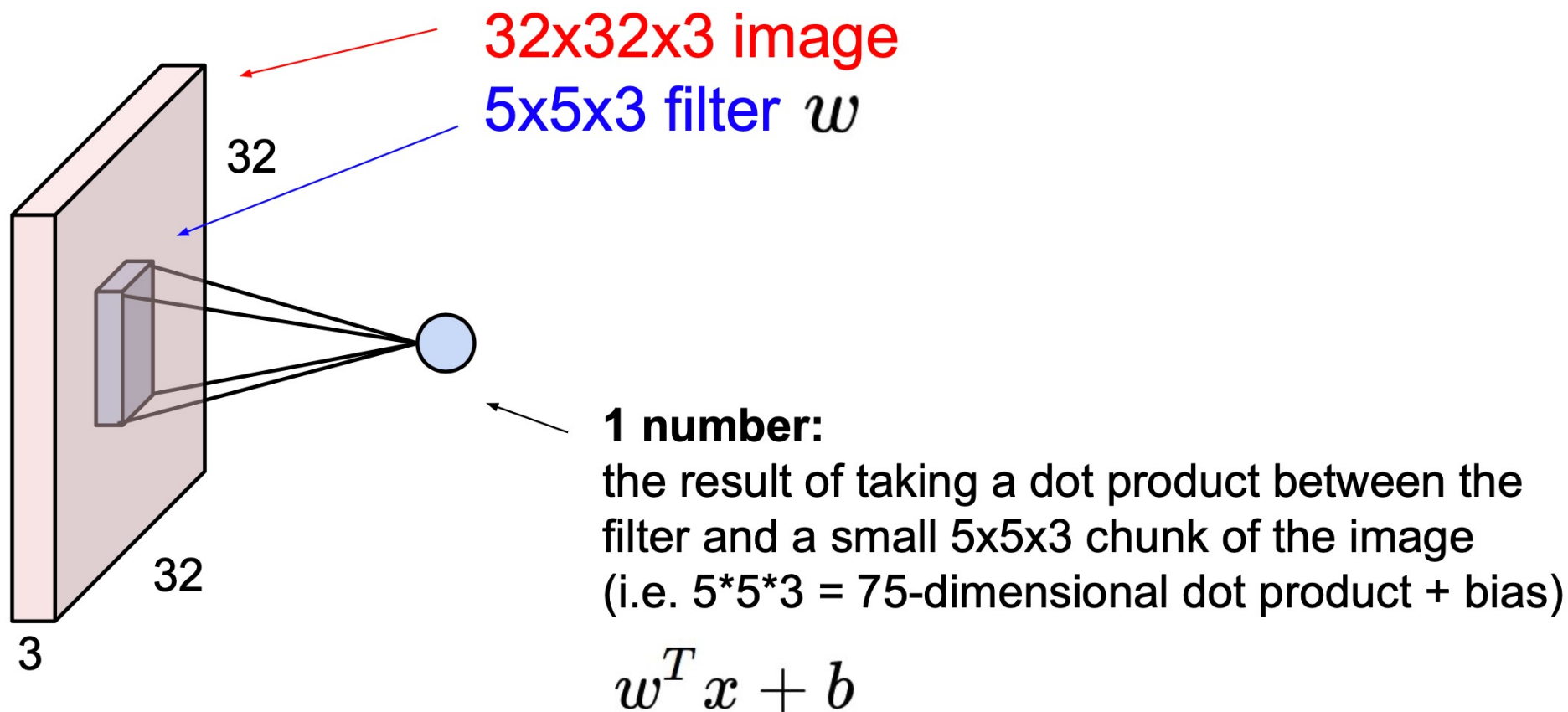
Filters always extend the full depth of the input volume

5x5x3 filter



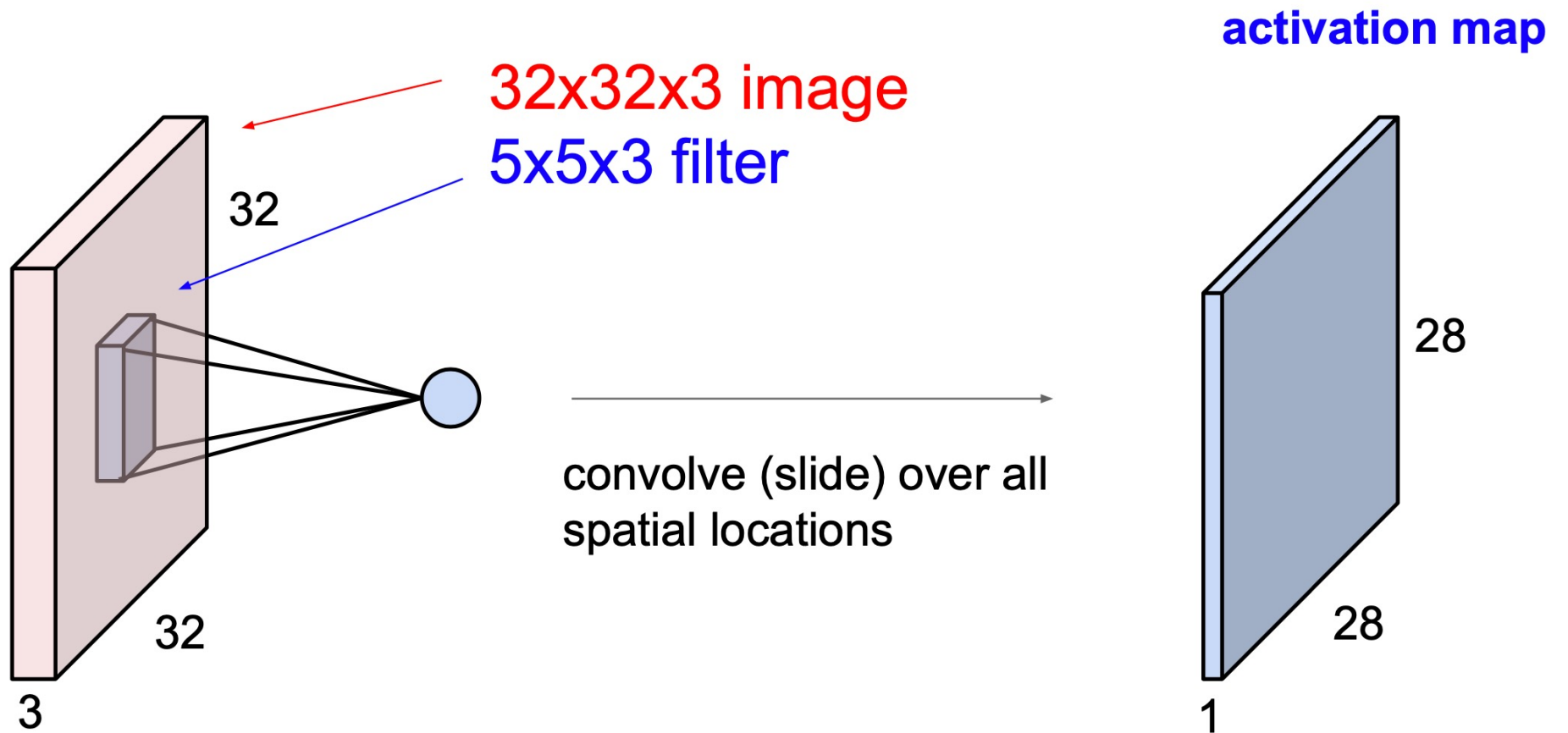
**Convolve** the filter with the image  
i.e. “slide over the image spatially,  
computing dot products”

# Convolution Layer





# Convolution Layer

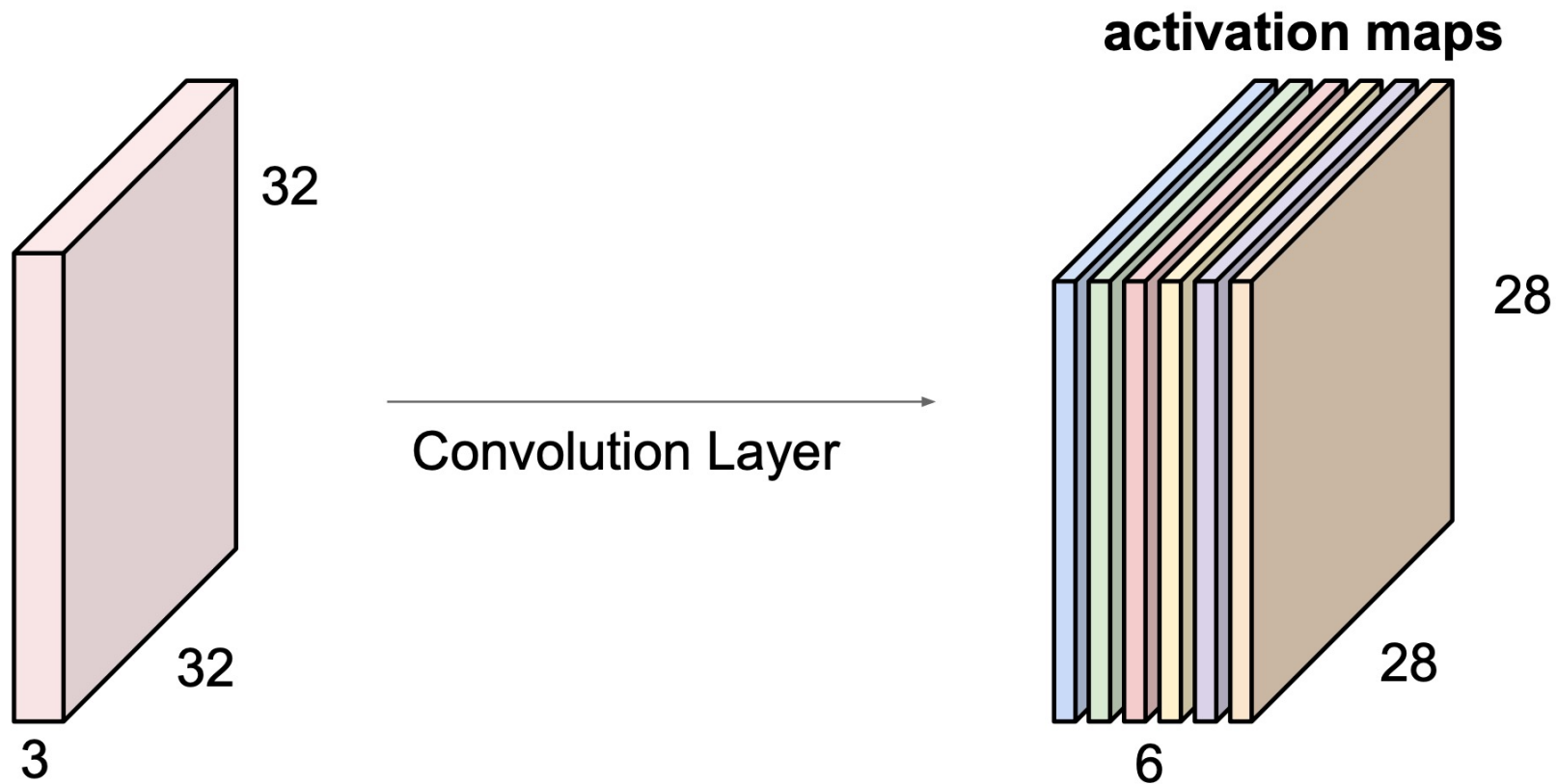


# Convolution Layer

consider a second, **green** filter

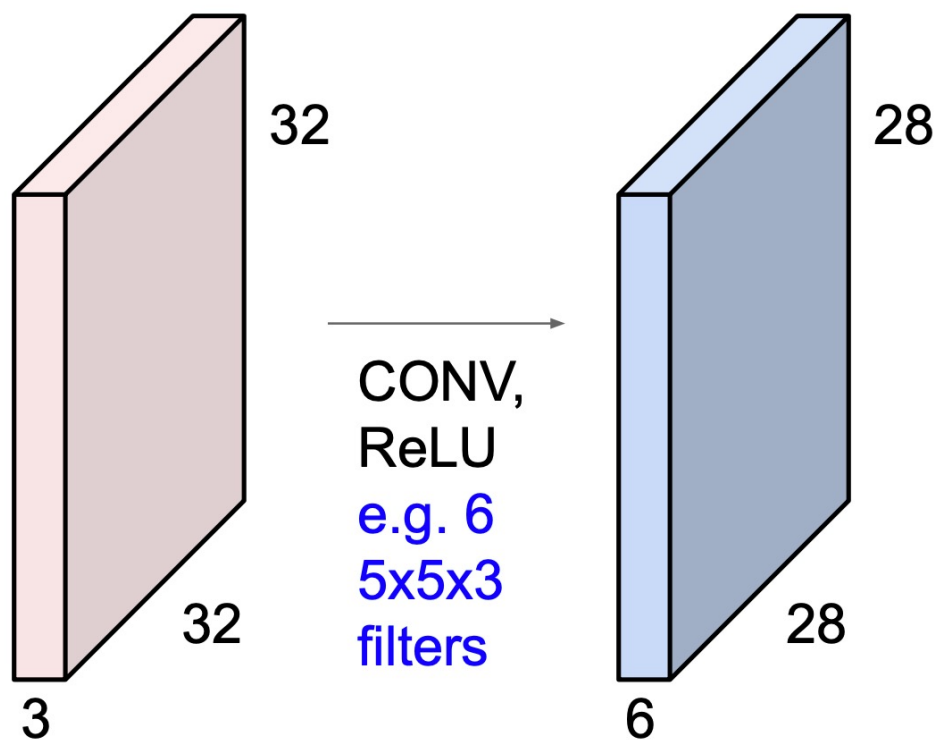


For example, if we had 6 5x5 filters, we'll get 6 separate activation maps:

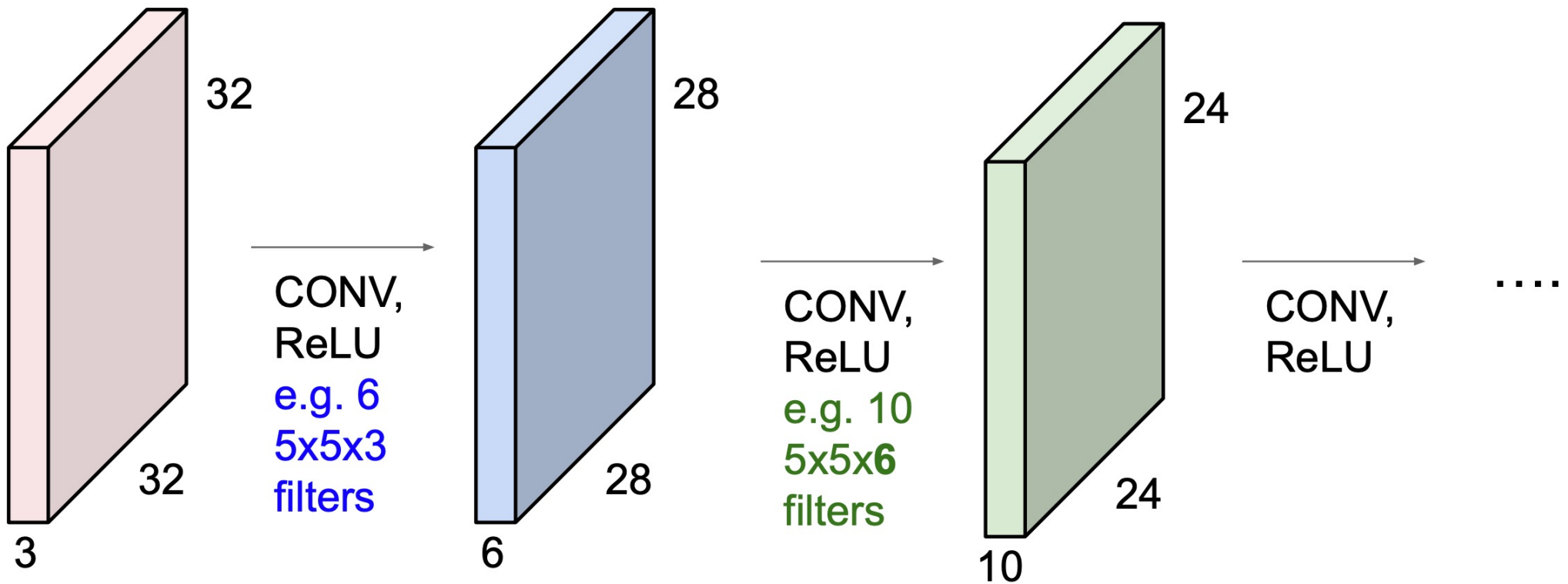


We stack these up to get a “new image” of size 28x28x6!

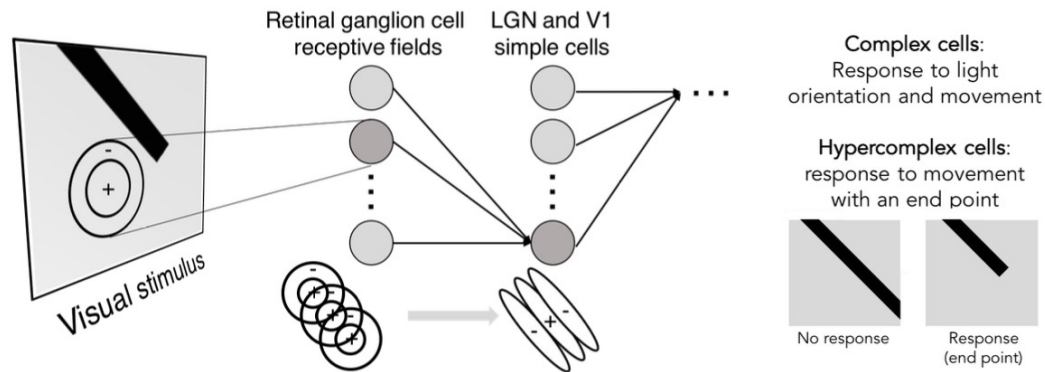
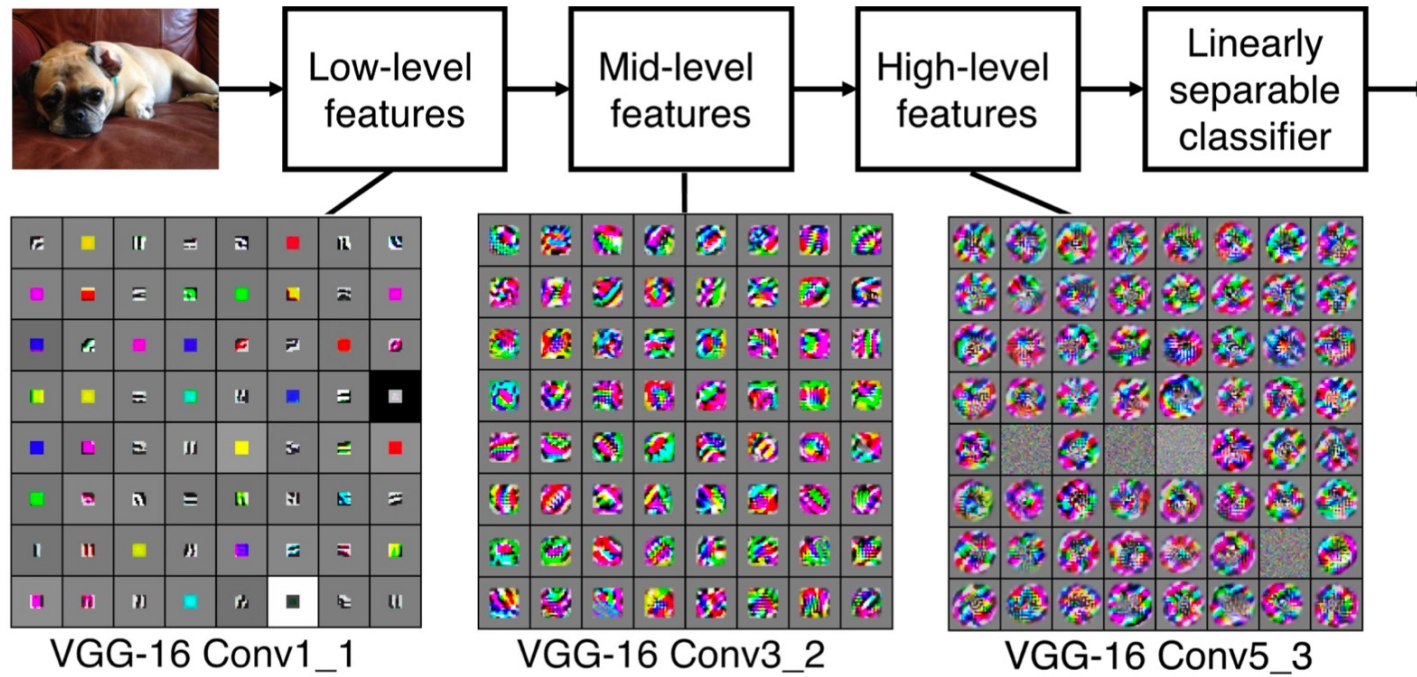
**Preview:** ConvNet is a sequence of Convolution Layers, interspersed with activation functions



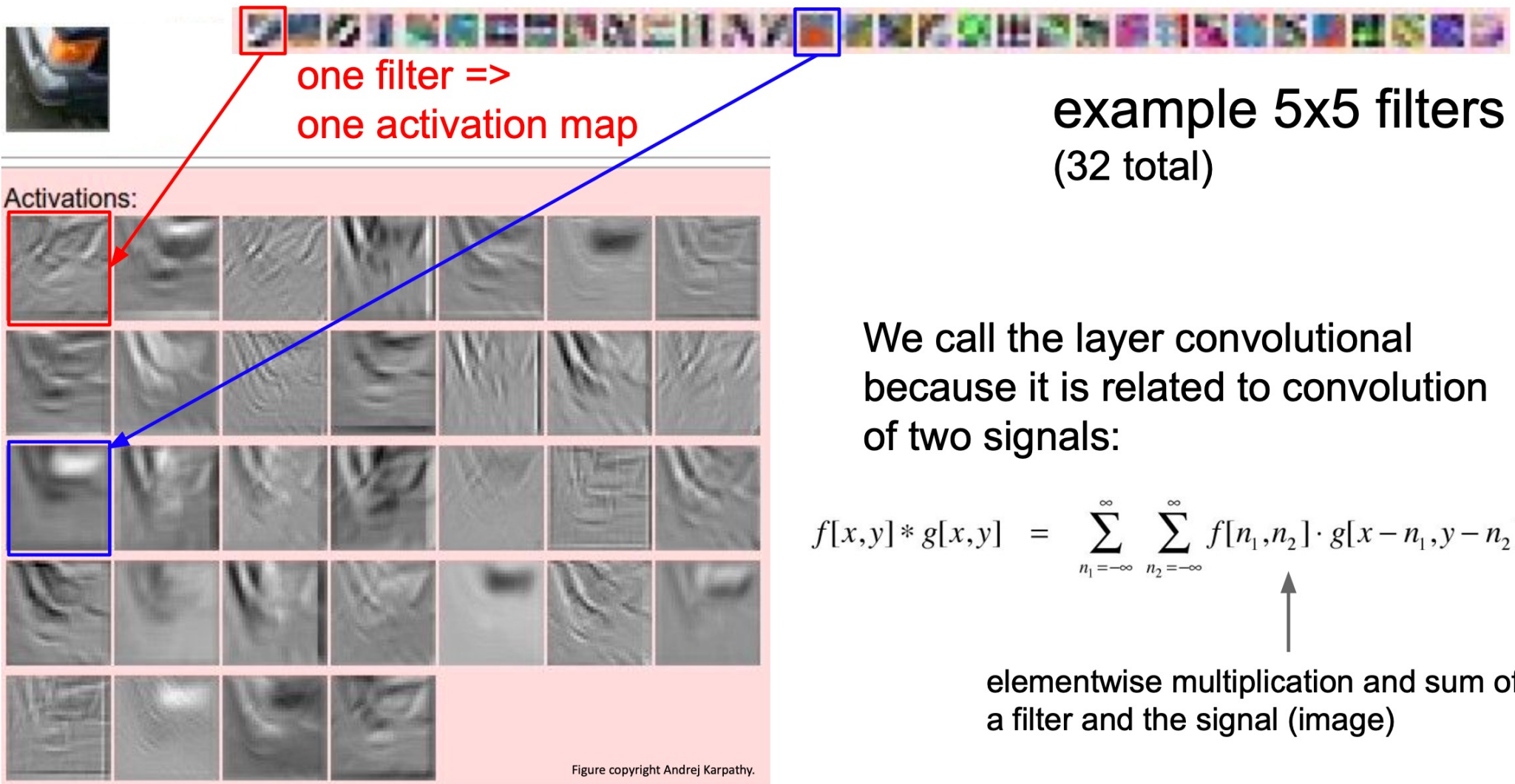
**Preview:** ConvNet is a sequence of Convolution Layers, interspersed with activation functions



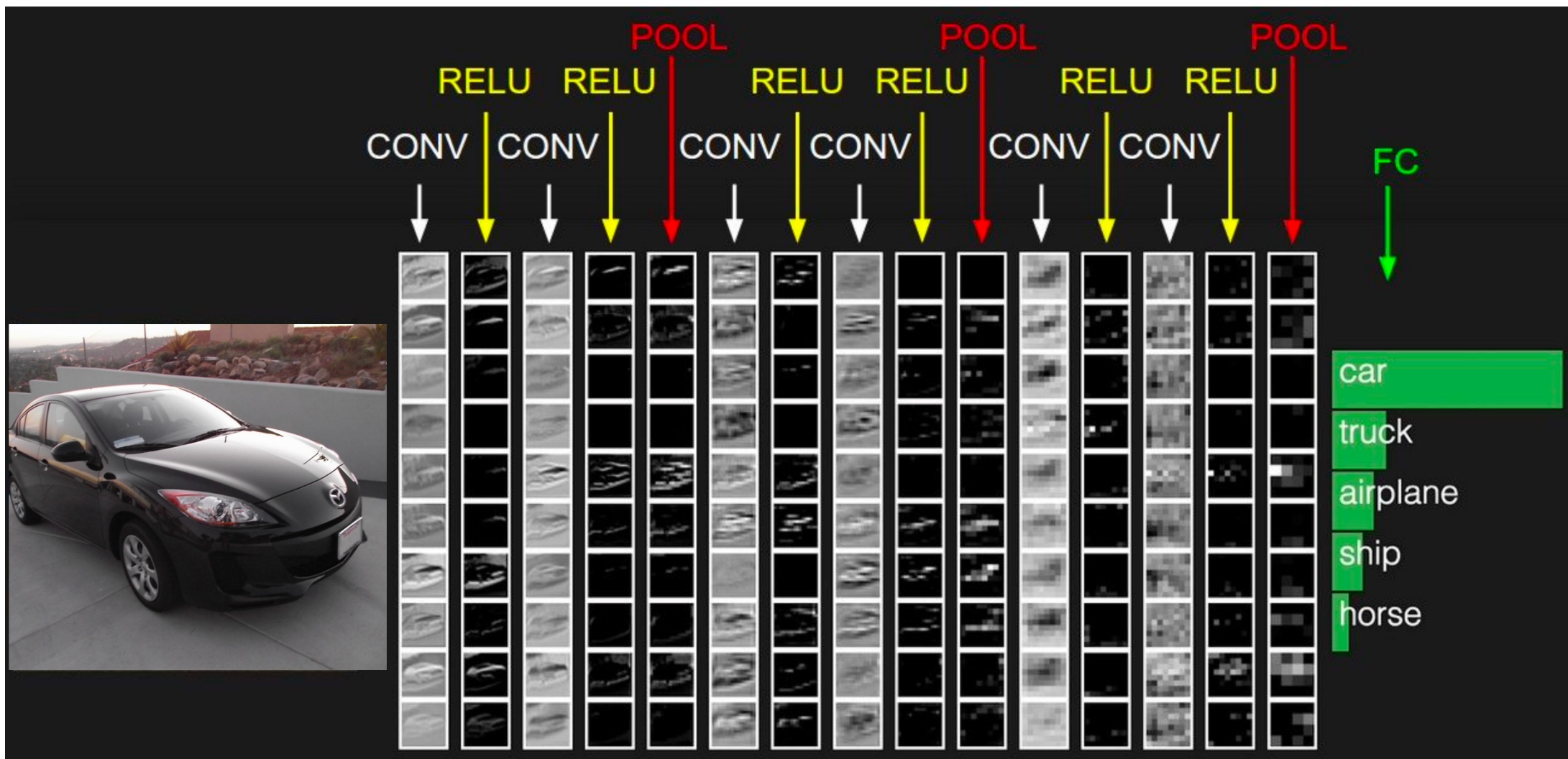
# Preview





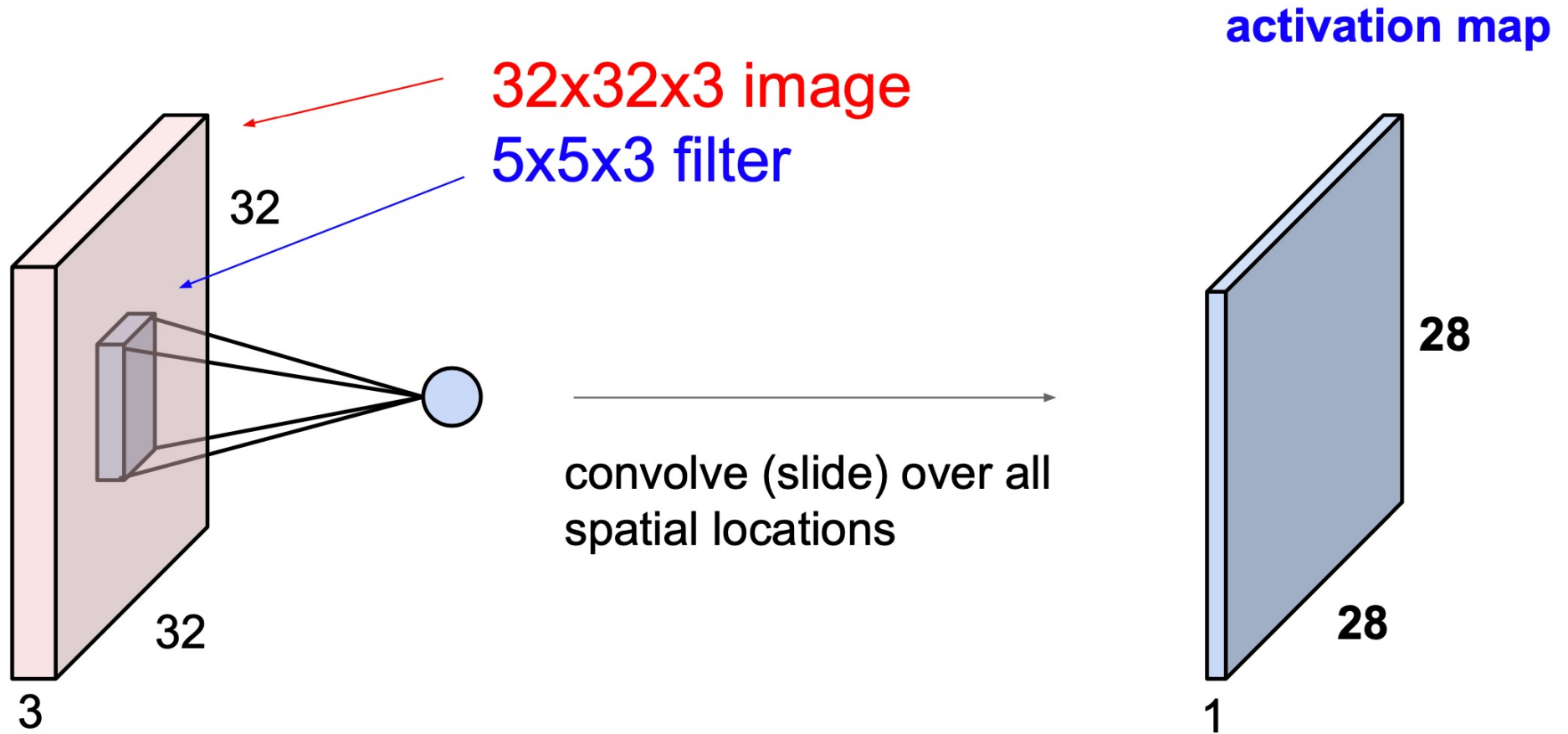


preview:



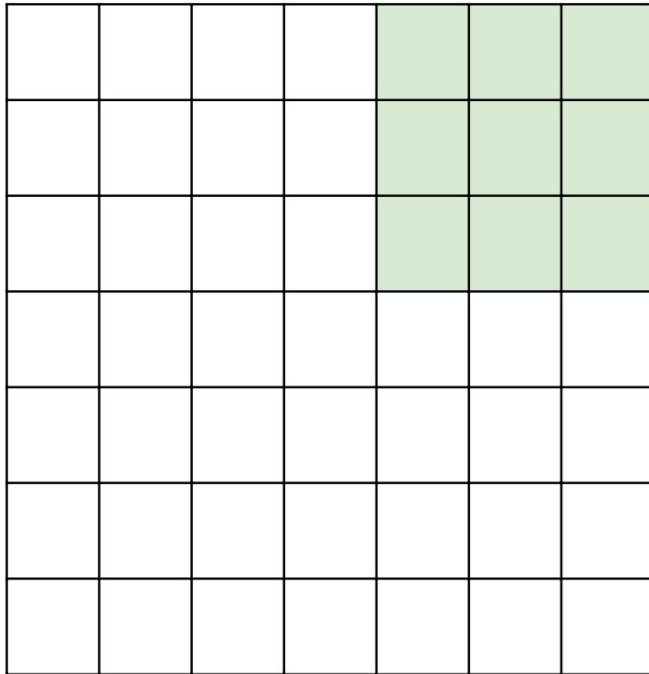


A closer look at spatial dimensions:



A closer look at spatial dimensions:

7

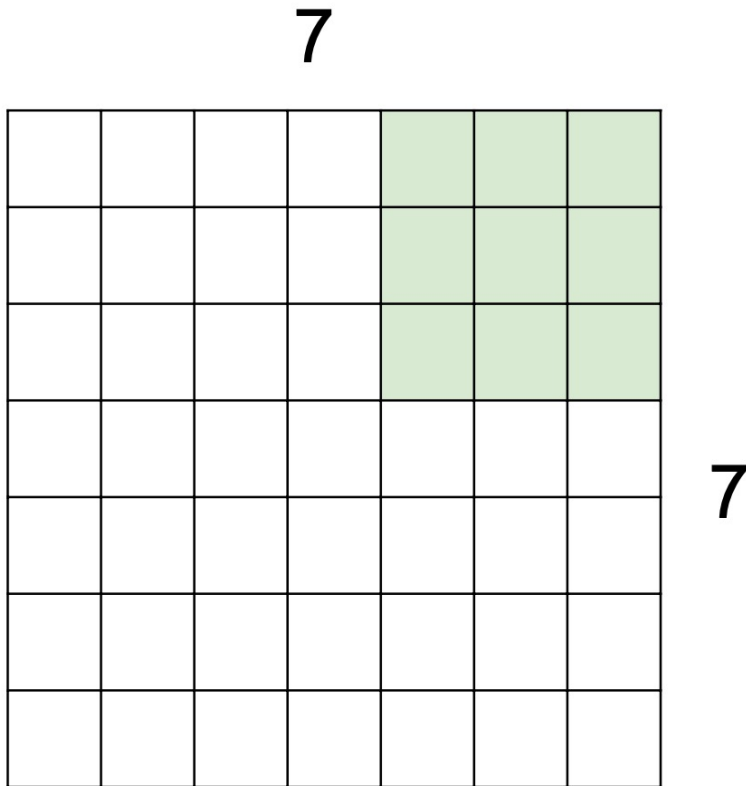


7

7x7 input (spatially)  
assume 3x3 filter

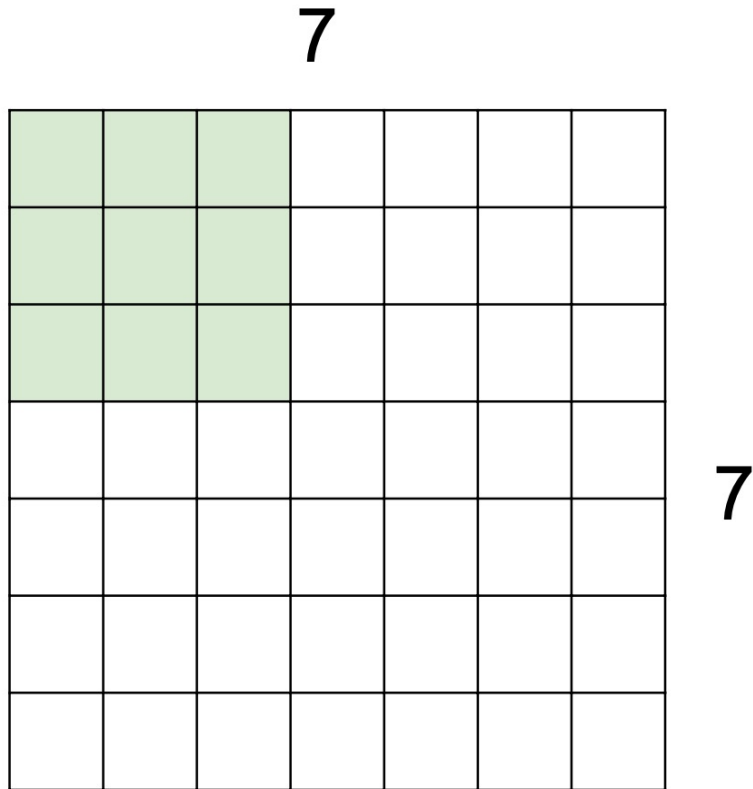
**=> 5x5 output**

A closer look at spatial dimensions:



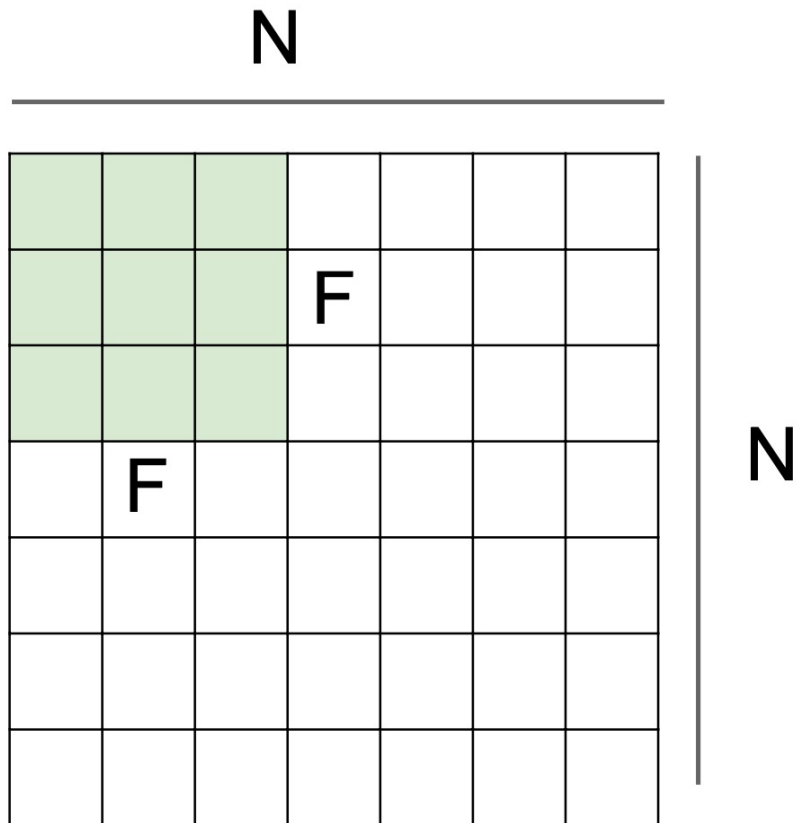
7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 2**  
**=> 3x3 output!**

A closer look at spatial dimensions:



7x7 input (spatially)  
assume 3x3 filter  
applied **with stride 3?**

**doesn't fit!**  
cannot apply 3x3 filter on  
7x7 input with stride 3.



Output size:  
 **$(N - F) / \text{stride} + 1$**

e.g.  $N = 7, F = 3$ :

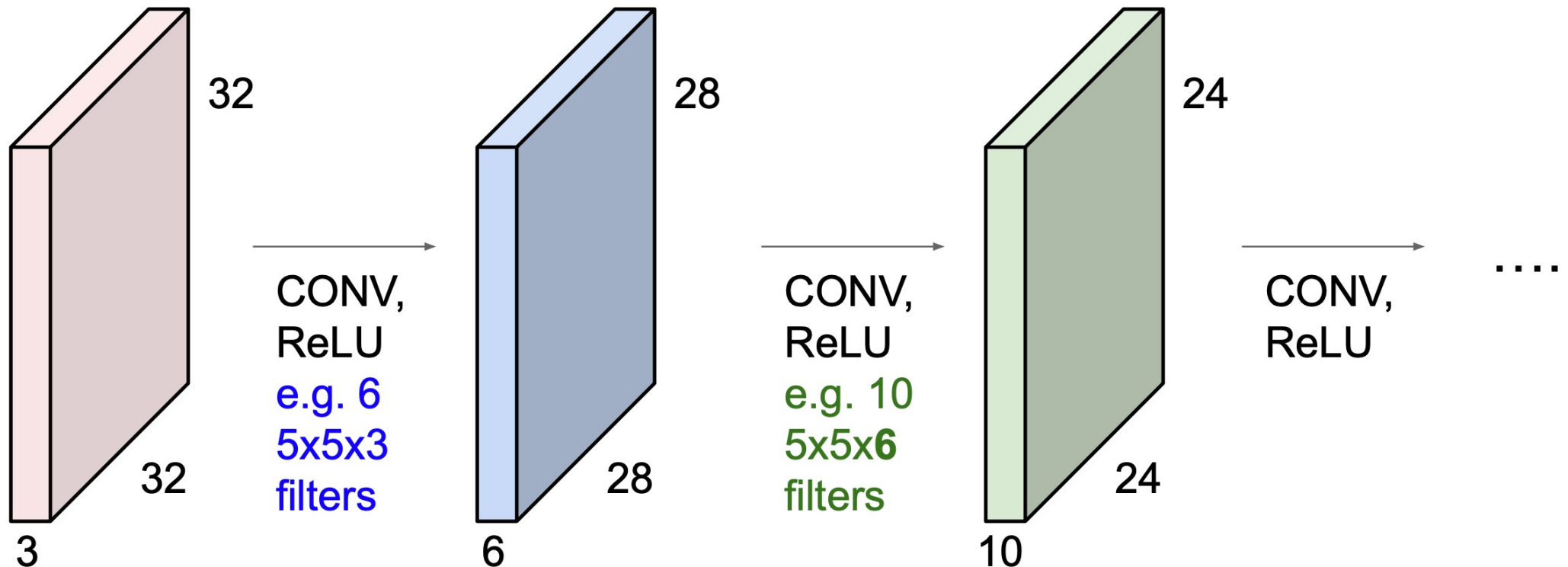
stride 1  $\Rightarrow (7 - 3)/1 + 1 = 5$

stride 2  $\Rightarrow (7 - 3)/2 + 1 = 3$

stride 3  $\Rightarrow (7 - 3)/3 + 1 = 2.33 \therefore \backslash$

## Remember back to...

E.g. 32x32 input convolved repeatedly with 5x5 filters shrinks volumes spatially! (32 -> 28 -> 24 ...). Shrinking too fast is not good, doesn't work well.



## In practice: Common to zero pad the border

|   |   |   |   |   |   |  |  |  |
|---|---|---|---|---|---|--|--|--|
| 0 | 0 | 0 | 0 | 0 | 0 |  |  |  |
| 0 |   |   |   |   |   |  |  |  |
| 0 |   |   |   |   |   |  |  |  |
| 0 |   |   |   |   |   |  |  |  |
| 0 |   |   |   |   |   |  |  |  |
|   |   |   |   |   |   |  |  |  |
|   |   |   |   |   |   |  |  |  |
|   |   |   |   |   |   |  |  |  |
|   |   |   |   |   |   |  |  |  |

e.g. input 7x7

**3x3** filter, applied with **stride 1**

**pad with 1 pixel** border => what is the output?

**7x7 output!**

(recall:)

$$(N + 2P - F) / \text{stride} + 1$$

## In practice: Common to zero pad the border

|   |   |   |   |   |   |  |  |  |
|---|---|---|---|---|---|--|--|--|
| 0 | 0 | 0 | 0 | 0 | 0 |  |  |  |
| 0 |   |   |   |   |   |  |  |  |
| 0 |   |   |   |   |   |  |  |  |
| 0 |   |   |   |   |   |  |  |  |
| 0 |   |   |   |   |   |  |  |  |
|   |   |   |   |   |   |  |  |  |
|   |   |   |   |   |   |  |  |  |
|   |   |   |   |   |   |  |  |  |
|   |   |   |   |   |   |  |  |  |

e.g. input 7x7

**3x3** filter, applied with **stride 1**

**pad with 1 pixel** border => what is the output?

**7x7 output!**

in general, common to see CONV layers with stride 1, filters of size  $F \times F$ , and zero-padding with  $(F-1)/2$ . (will preserve size spatially)

e.g.  $F = 3 \Rightarrow$  zero pad with 1

$F = 5 \Rightarrow$  zero pad with 2

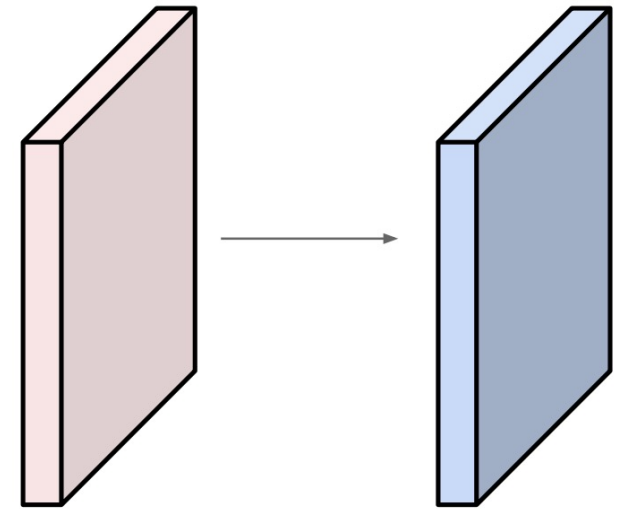
$F = 7 \Rightarrow$  zero pad with 3



Examples time:

Input volume: **32x32x3**  
10 5x5 filters with stride 1, pad 2

Output volume size: ?



Examples time:

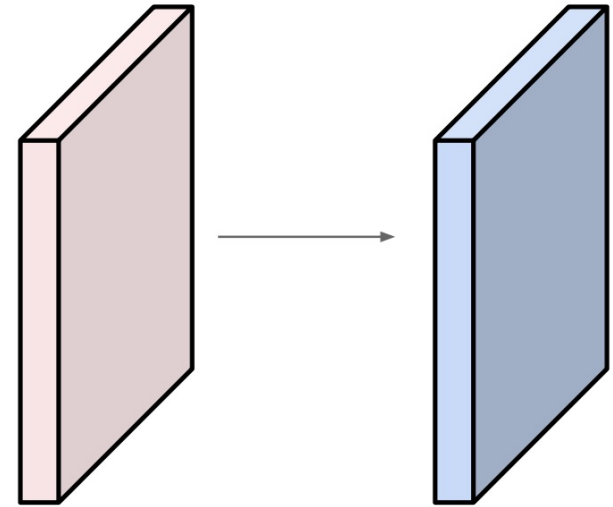
Input volume: **32x32x3**

**10** **5x5** filters with stride **1**, pad **2**

Output volume size:

$(32 + 2 * 2 - 5) / 1 + 1 = 32$  spatially, so

**32x32x10**

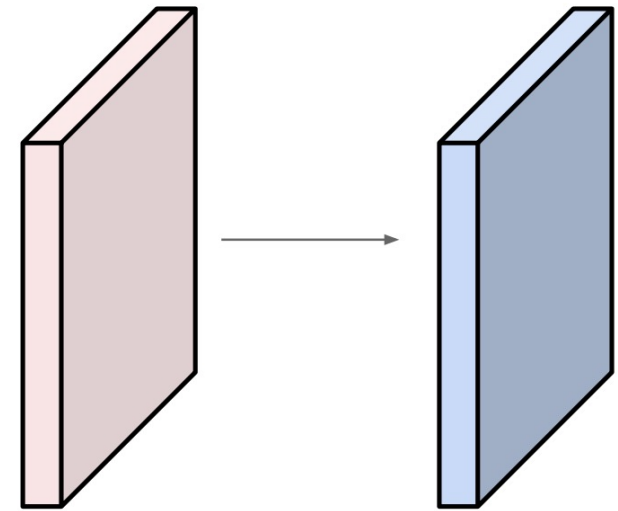


Examples time:

Input volume: **32x32x3**

10 5x5 filters with stride 1, pad 2

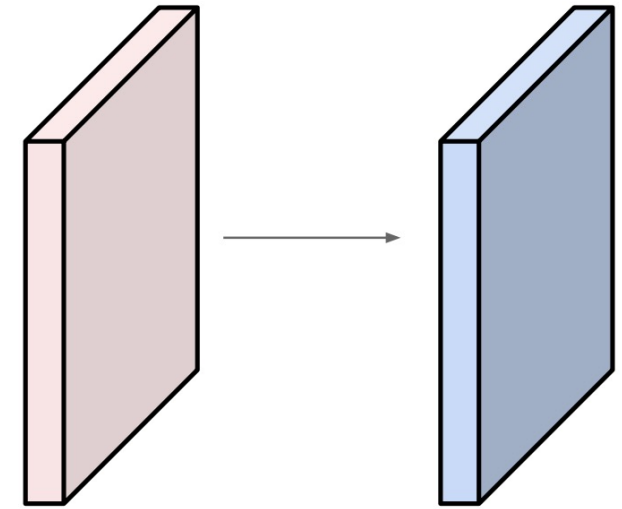
Number of parameters in this layer?



Examples time:

Input volume: **32x32x3**

**10** **5x5** filters with stride 1, pad 2



Number of parameters in this layer?

each filter has  $5*5*3 + 1 = 76$  params (+1 for bias)

=>  $76*10 = 760$

# Convolution layer: summary

## Common settings:

Let's assume input is  $W_1 \times H_1 \times C$

Conv layer needs 4 hyperparameters:

- Number of filters **K**
- The filter size **F**
- The stride **S**
- The zero padding **P**

**K** = (powers of 2, e.g. 32, 64, 128, 512)

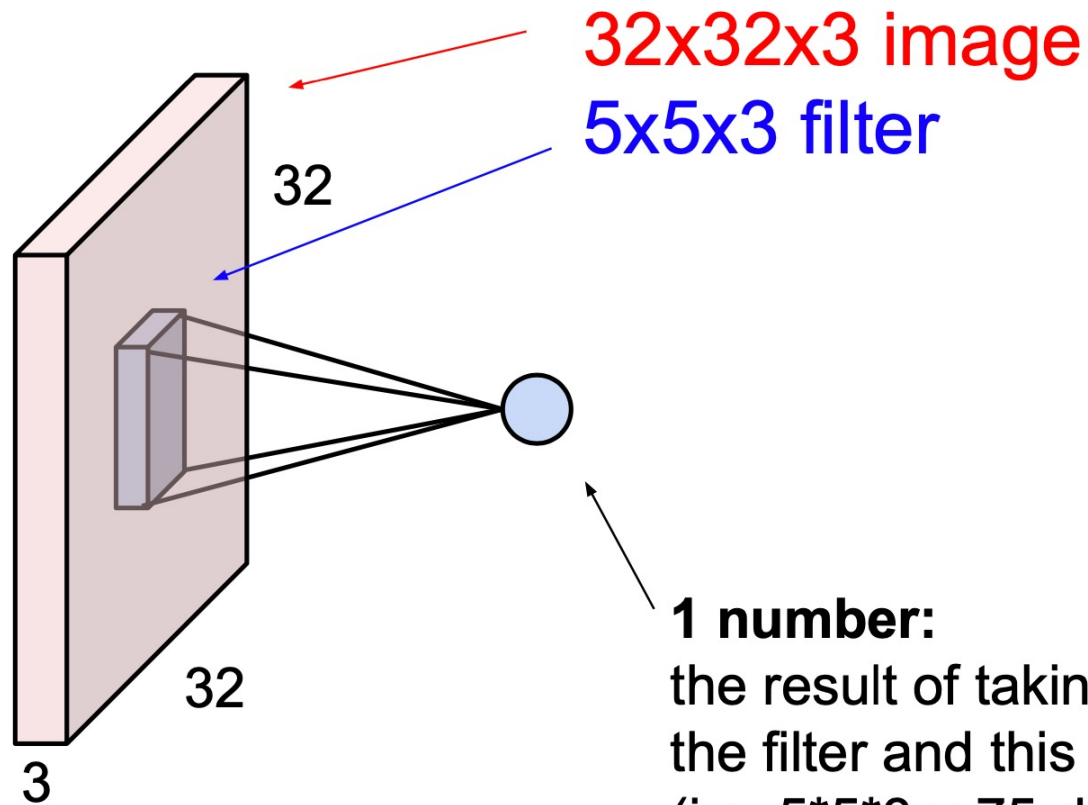
- **F** = 3, **S** = 1, **P** = 1
- **F** = 5, **S** = 1, **P** = 2
- **F** = 5, **S** = 2, **P** = ? (whatever fits)
- **F** = 1, **S** = 1, **P** = 0

This will produce an output of  $W_2 \times H_2 \times K$   
where:

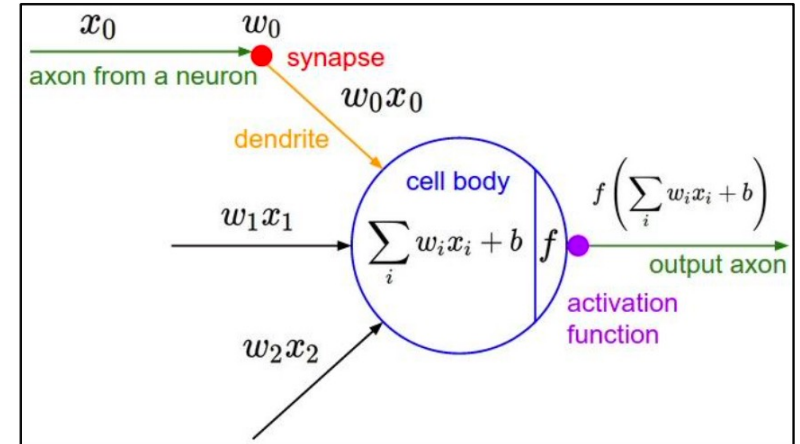
- $W_2 = (W_1 - F + 2P)/S + 1$
- $H_2 = (H_1 - F + 2P)/S + 1$

Number of parameters:  $F^2CK$  and **K** biases

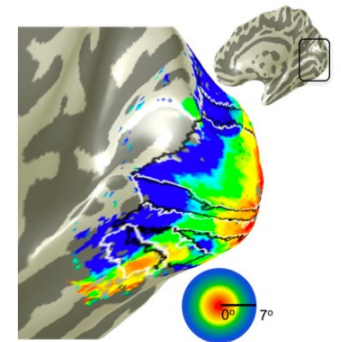
# The brain/neuron view of CONV Layer



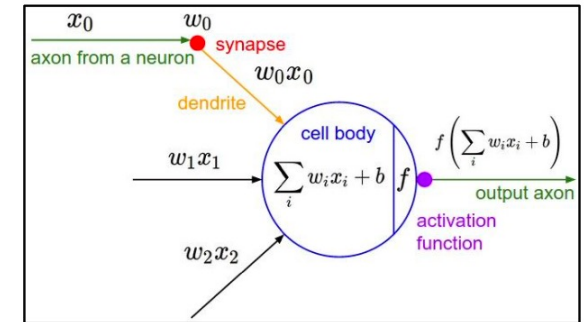
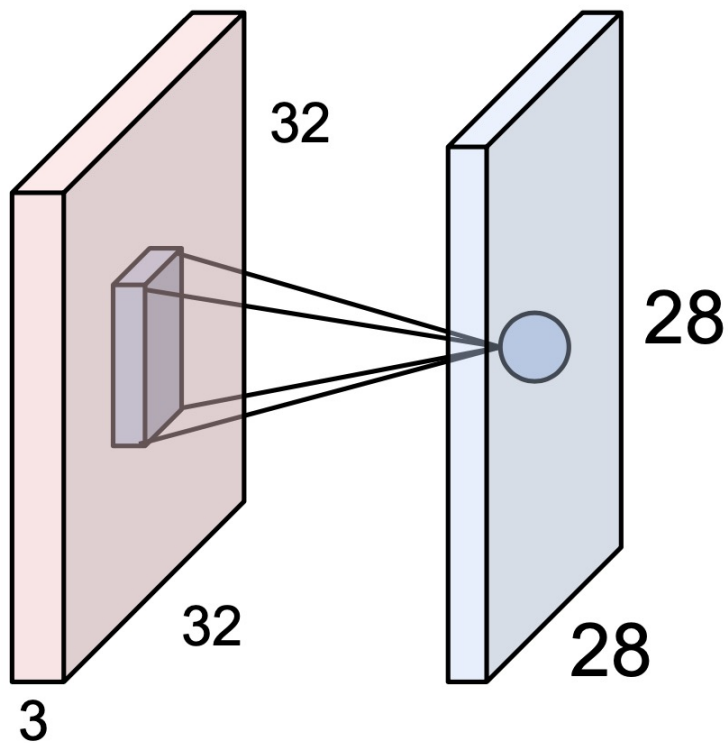
**1 number:**  
the result of taking a dot product between  
the filter and this part of the image  
(i.e.  $5 \times 5 \times 3 = 75$ -dimensional dot product)



It's just a neuron with local connectivity...



# Receptive field

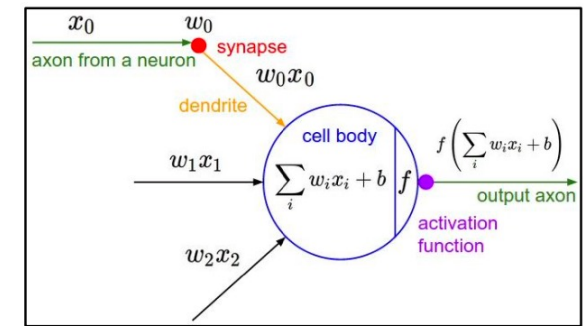
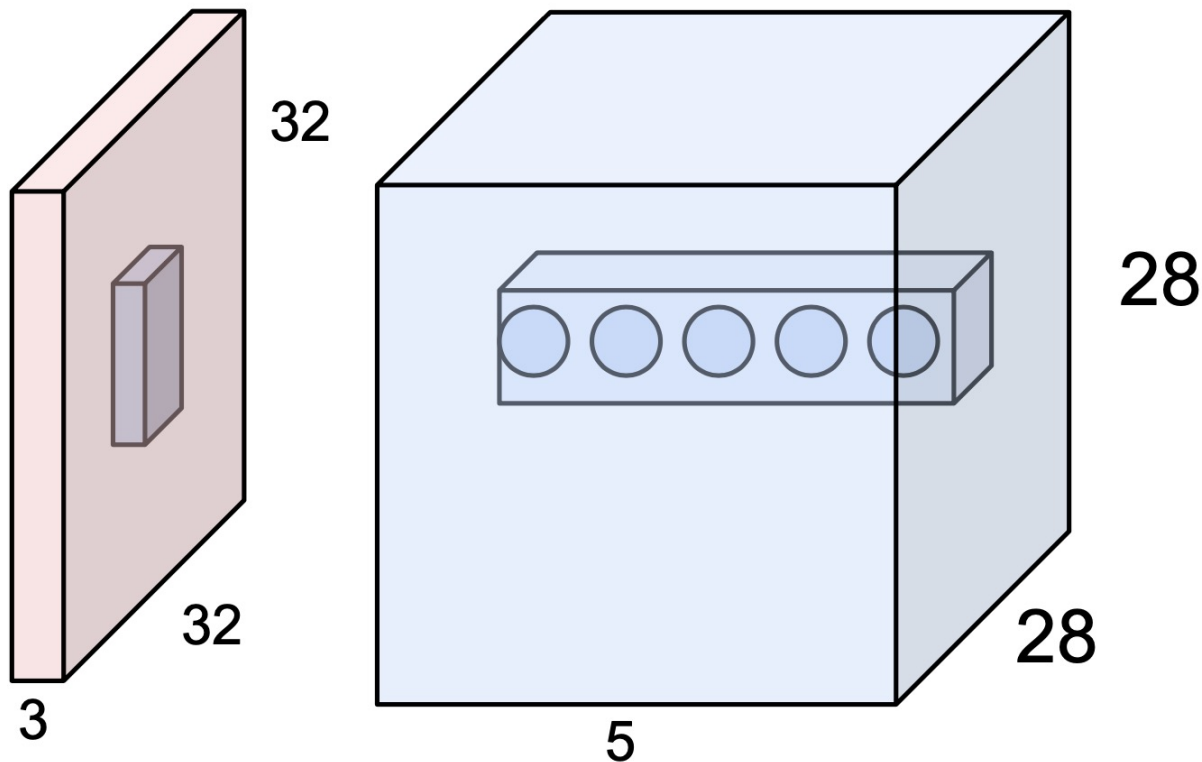


An activation map is a 28x28 sheet of neuron outputs:

1. Each is connected to a small region in the input
2. All of them share parameters

“5x5 filter” -> “5x5 receptive field for each neuron”

# The brain/neuron view of CONV Layer

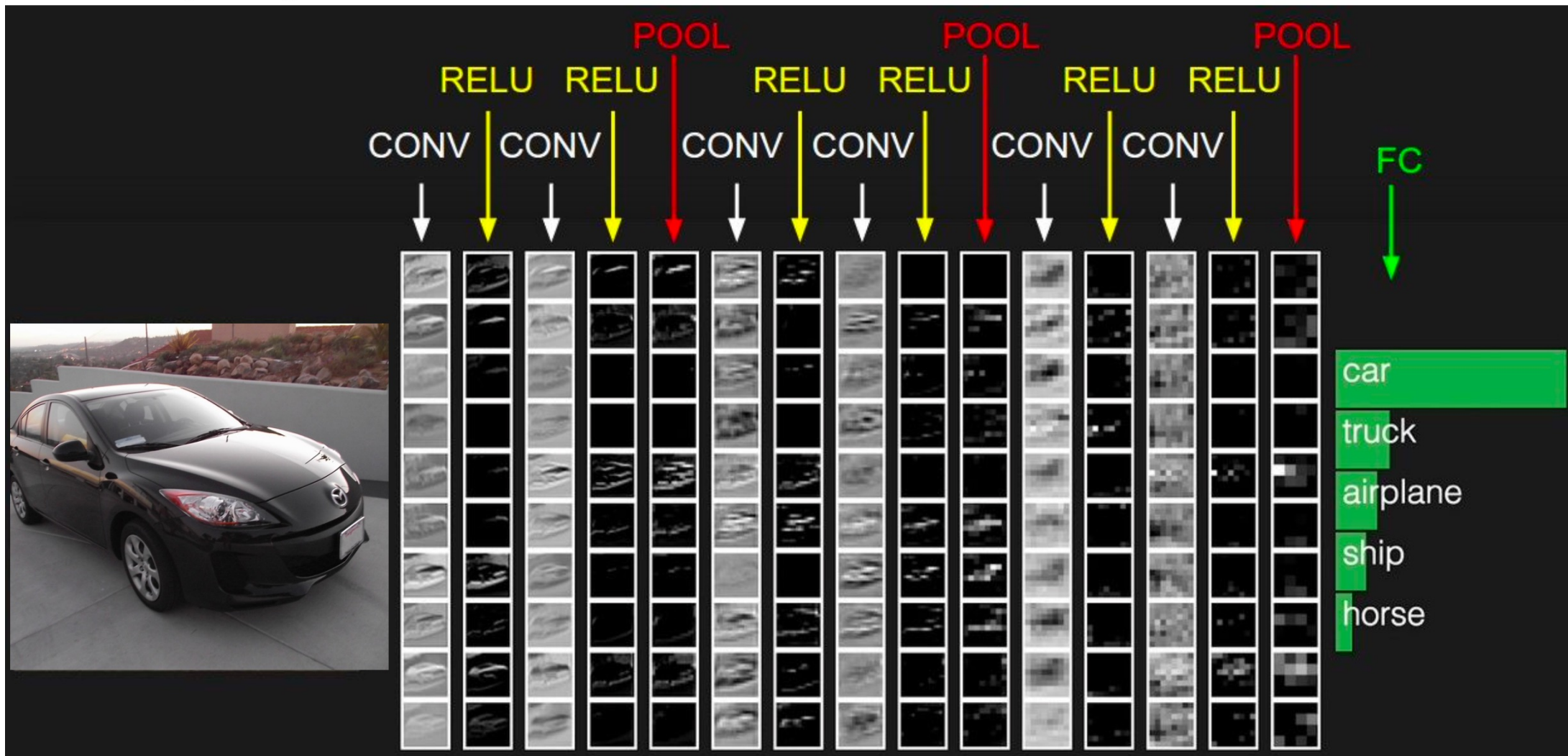


E.g. with 5 filters,  
CONV layer consists of  
neurons arranged in a 3D grid  
(28x28x5)

There will be 5 different  
neurons all looking at the same  
region in the input volume

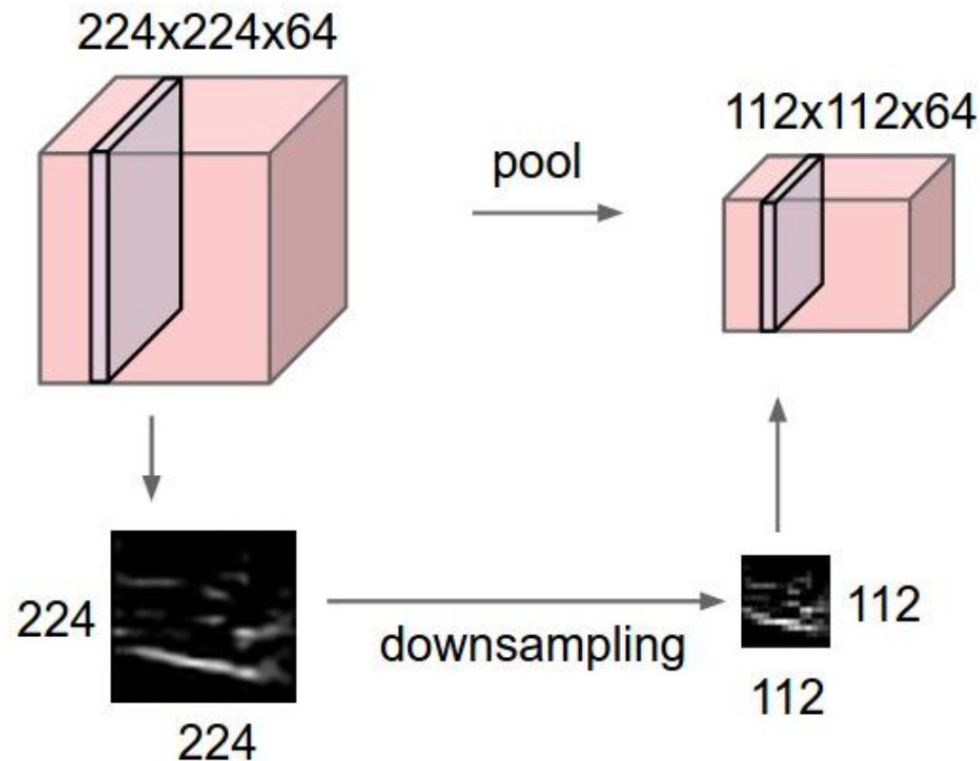


two more layers to go: POOL/FC



# Pooling layer

- makes the representations smaller and more manageable
- operates over each activation map independently:



# MAX POOLING

Single depth slice

|   |   |   |   |
|---|---|---|---|
| 1 | 1 | 2 | 4 |
| 5 | 6 | 7 | 8 |
| 3 | 2 | 1 | 0 |
| 1 | 2 | 3 | 4 |

max pool with 2x2 filters  
and stride 2



|   |   |
|---|---|
| 6 | 8 |
| 3 | 4 |

# Pooling layer: summary

Let's assume input is  $W_1 \times H_1 \times C$

Conv layer needs 2 hyperparameters:

- The spatial extent **F**
- The stride **S**

This will produce an output of  $W_2 \times H_2 \times C$  where:

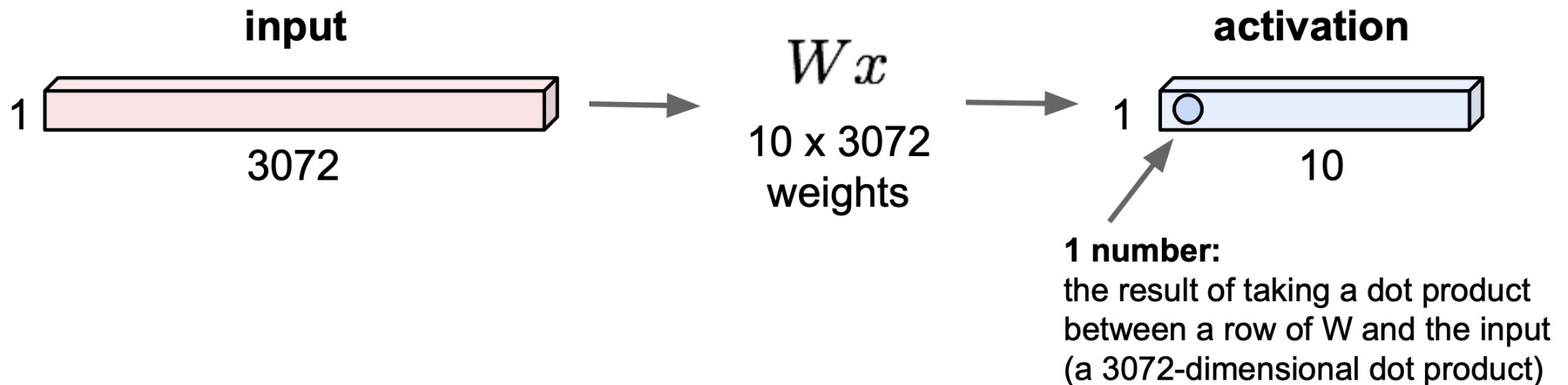
- $W_2 = (W_1 - F) / S + 1$
- $H_2 = (H_1 - F) / S + 1$

Number of parameters: 0

# Fully Connected Layer

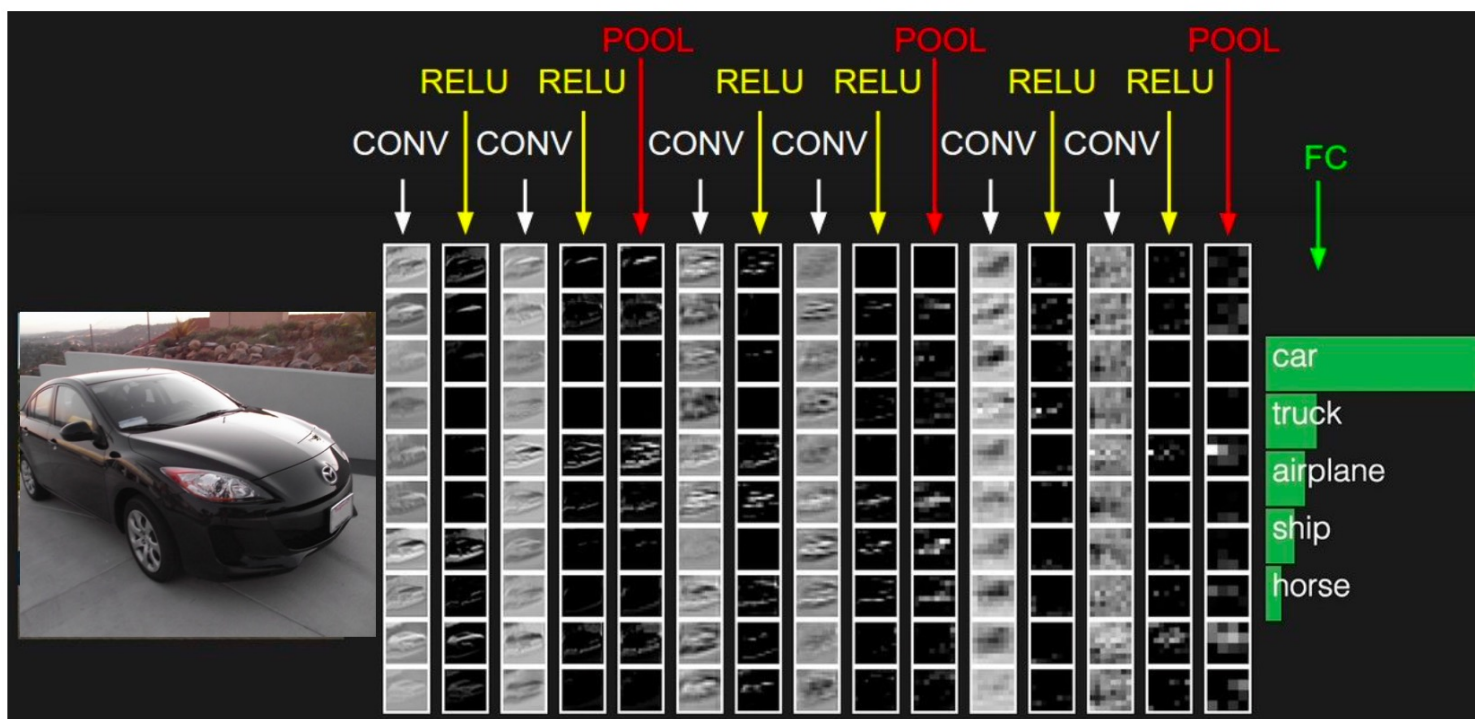
32x32x3 image -> stretch to 3072 x 1

Each neuron  
looks at the full  
input volume



# Fully Connected Layer (FC layer)

- Contains neurons that connect to the entire input volume, as in ordinary Neural Networks





# Summary

- ConvNets stack CONV, POOL, FC layers
- Trend towards smaller filters and deeper architectures
- Trend towards getting rid of POOL/FC layers (just CONV)
- Historically architectures looked like  
 **$[(\text{CONV-RELU}) * N - \text{POOL?}] * M - (\text{FC-RELU}) * K, \text{SOFTMAX}$**   
where N is usually up to ~5, M is large,  $0 \leq K \leq 2$ .
  - but recent advances such as ResNet/GoogLeNet have challenged this paradigm



# END